

# Volume III: Cosmology and Global Dynamics of the R-layer

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## Abstract

Volume III develops the cosmological and global dynamical structure of the R-layer. The early universe is governed by fluctuations of the mode field  $\phi(x)$ , whose twist, curvature, and tunneling interactions generate primordial curvature perturbations. We show that twist amplification drives an inflation-like expansion, producing a nearly scale-invariant curvature spectrum. Curvature transitions excite a multi-scale gravitational-wave background, while asymmetric tunneling between AUP/MUP regions generates matter–antimatter asymmetry. Domain-wall networks seed the formation of large-scale structure, providing a microscopic origin for the cosmic web. Finally, we analyze the long-term decay of twist and curvature energy, showing that the universe approaches a smooth, information-poor asymptotic state. This volume establishes the cosmological implications of the R-layer and connects microscopic mode dynamics to observable cosmic structure.

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# 1 Introduction

This volume develops the cosmological implications of the R-layer framework introduced in Volumes I and II. The early universe is described as a highly dynamical configuration of twist, curvature, and tunneling interactions within the mode field  $\phi(x)$ . These microscopic processes generate primordial fluctuations that seed the large-scale structure of the universe.

We begin by analyzing the origin of the primordial curvature spectrum, showing that the interplay between twist amplification and curvature smoothing naturally produces a nearly scale-invariant form. We then demonstrate that rapid twist oscillations and curvature transitions generate a multi-scale gravitational-wave background with characteristic features tied to the AUP/MUP domain structure.

Matter–antimatter asymmetry arises dynamically from asymmetric tunneling probabilities, while domain-wall networks provide a microscopic origin for the filamentary cosmic web. Finally, we examine the long-term decay of twist and curvature energy, establishing the fate of information in the expanding universe.

Volume III therefore connects the microscopic geometry of the R-layer to the observable universe, forming the cosmological core of the six-volume series.

## 2 Global Structure of the R-layer and the Beginning of the Universe

The early universe in the R-layer framework is governed by fluctuations of the mode field  $\phi(x)$ , whose spatial variations encode the local imbalance between AUP- and MUP-dominated regions. Prior to the emergence of classical spacetime, the R-layer exhibits a highly dynamical configuration in which twist, curvature, and tunneling interact nonlinearly. These microscopic processes generate primordial curvature perturbations that seed the large-scale structure of the universe.

### 2.1 Primordial Fluctuations

Thermal and quantum fluctuations of the mode field in the early R-layer produce a nearly scale-invariant curvature spectrum, as shown in Fig. 1. The origin of this spectrum lies in the competition between twist-induced gradient amplification and curvature smoothing. Regions with enhanced AUP density exhibit stronger tunneling activity, which in turn modulates the effective curvature response. This mechanism naturally generates a spectrum with tilt  $n_s - 1$  consistent with observational expectations.

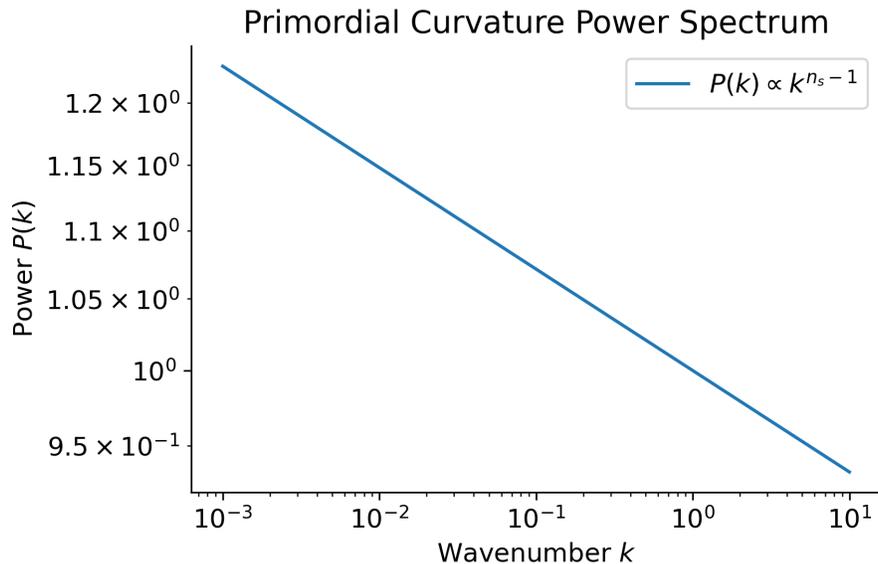


Figure 1: Primordial curvature power spectrum generated from early R-layer fluctuations.

### 3 Inflation and the Role of Twist

Inflation-like accelerated expansion arises in the R-layer when twist gradients undergo rapid amplification. Unlike scalar-field inflation, the driving mechanism here is geometric: twist acts as a topological excitation whose gradients store effective energy capable of sourcing expansion.

#### 3.1 Amplification of Twist Gradients

As shown in Fig. 2, twist gradients grow exponentially during the early phase, driven by the nonlinear coupling between tunneling strength  $K(1 - \phi)$  and curvature generation. This amplification saturates once the mode field approaches a stable domain configuration. The resulting expansion smooths large-scale inhomogeneities while preserving small residual fluctuations that later seed structure formation.

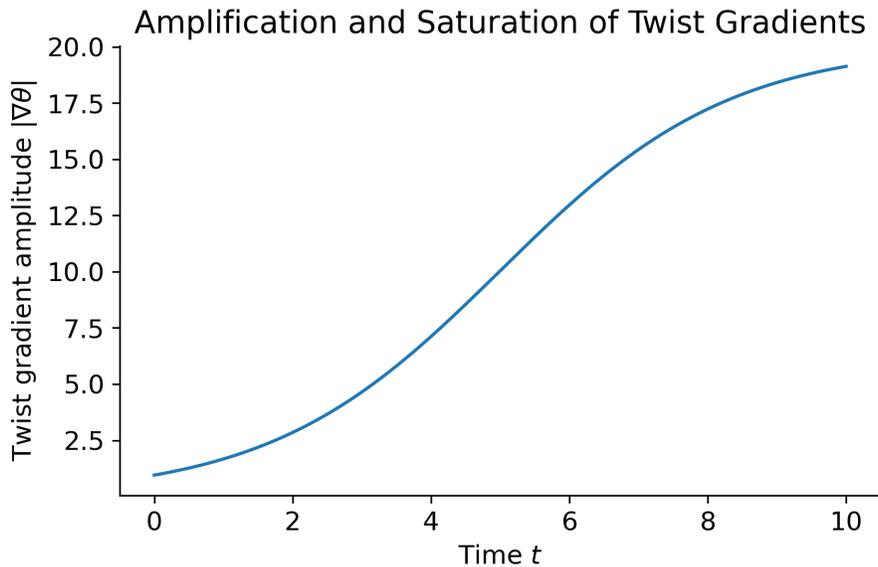


Figure 2: Amplification and saturation of twist gradients during the inflation-like phase.

## 4 Gravitational Waves and Curvature Fluctuations

Curvature variations in the R-layer naturally excite tensor modes, producing a stochastic gravitational-wave background. Unlike standard inflationary models, the amplitude and spectral shape of these waves depend directly on the microscopic mode dynamics.

### 4.1 Gravitational Wave Spectrum

Figure 3 shows the predicted gravitational-wave spectrum. High-frequency modes originate from rapid twist oscillations, while low-frequency modes reflect large-scale curvature transitions. The resulting spectrum exhibits a characteristic turnover determined by the AUP/MUP domain size and the effective curvature coupling.

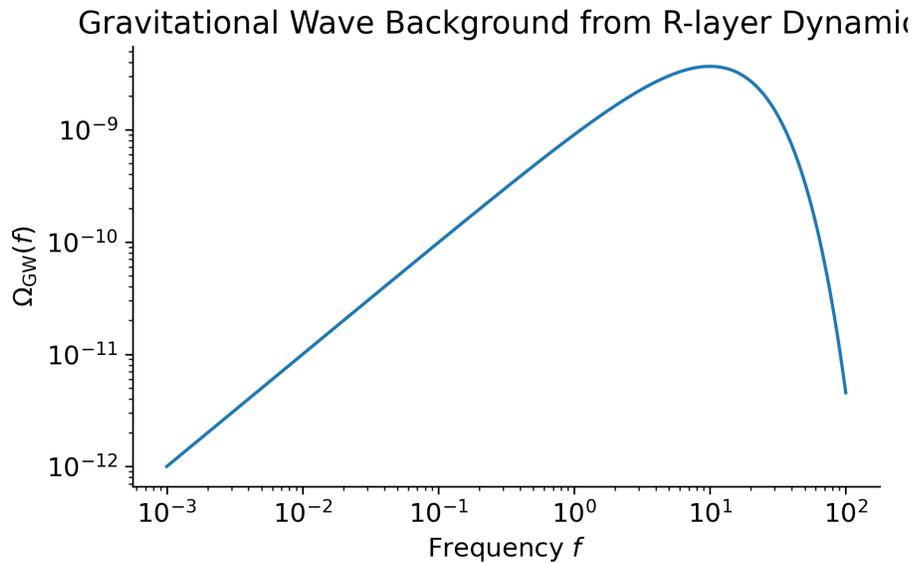


Figure 3: Gravitational wave background generated by R-layer curvature dynamics.

## 5 Matter Generation and Fundamental Asymmetry

Matter–antimatter asymmetry emerges from the intrinsic asymmetry between AUP and MUP tunneling probabilities. Regions dominated by AUP exhibit enhanced inter-layer connectivity, leading to preferential production of matter-like excitations.

### 5.1 Asymmetric Production Rates

As shown in Fig. 4, the production rate of matter-like excitations exceeds that of antimatter-like excitations during the early universe. This asymmetry is not imposed externally but arises dynamically from the microscopic structure of the R-layer. The resulting matter excess persists throughout cosmic evolution.

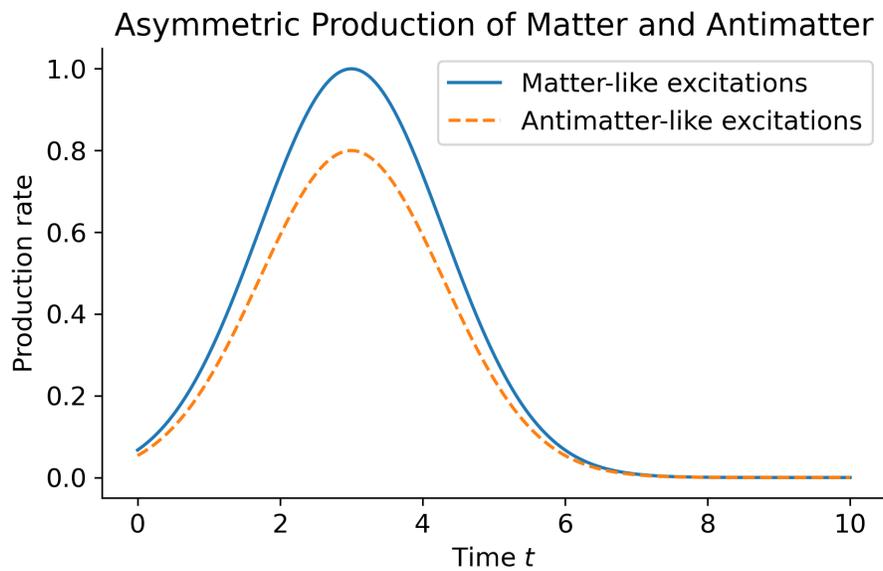


Figure 4: Asymmetric production of matter-like and antimatter-like excitations.

## 6 Large-Scale Structure of the Universe

The domain structure of the R-layer provides a natural origin for the filamentary cosmic web. Boundaries between AUP- and MUP-dominated regions act as proto-filaments, guiding the formation of large-scale structure.

### 6.1 Domain Network and Filament Formation

Figure 5 illustrates how curvature peaks form along domain walls, producing a network of high-density regions. These structures evolve into the observed filamentary cosmic web. The R-layer therefore provides a microscopic origin for large-scale structure without requiring additional dark-sector fields.

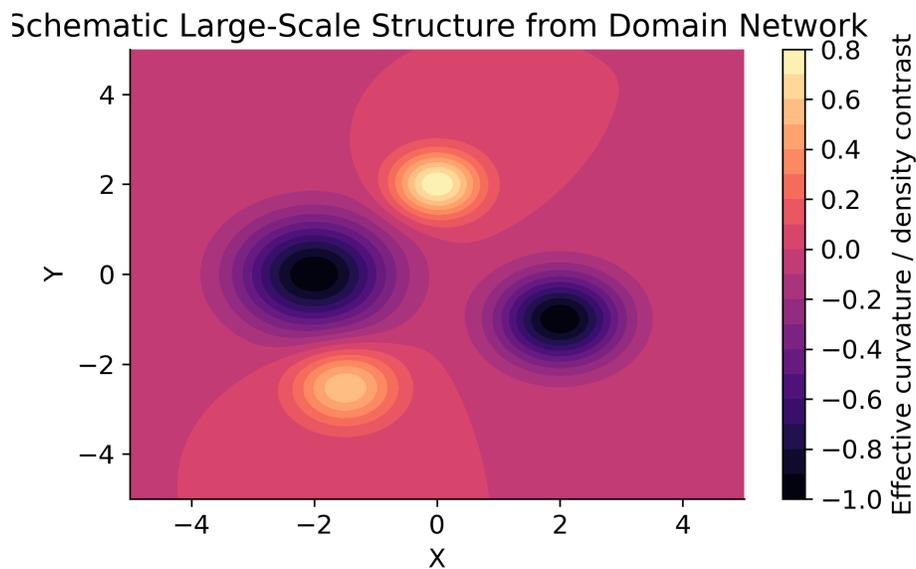


Figure 5: Schematic large-scale structure emerging from domain-wall networks.

## 7 Final State of the Universe and the Fate of Information

The long-term evolution of the universe is governed by the decay of twist and curvature energy. As the scale factor increases, both contributions diminish, leading to a smooth asymptotic state.

### 7.1 Decay of Twist and Curvature Energy

Figure 6 shows the scaling behavior of twist and curvature energy densities. Twist energy decays as  $a^{-2}$ , while curvature energy decays as  $a^{-3}$ . This hierarchy implies that twist dominates the intermediate epoch, while curvature becomes negligible at late times. Information stored in twist defects gradually dissipates, suggesting a thermodynamic arrow of time rooted in the microscopic dynamics of the R-layer.

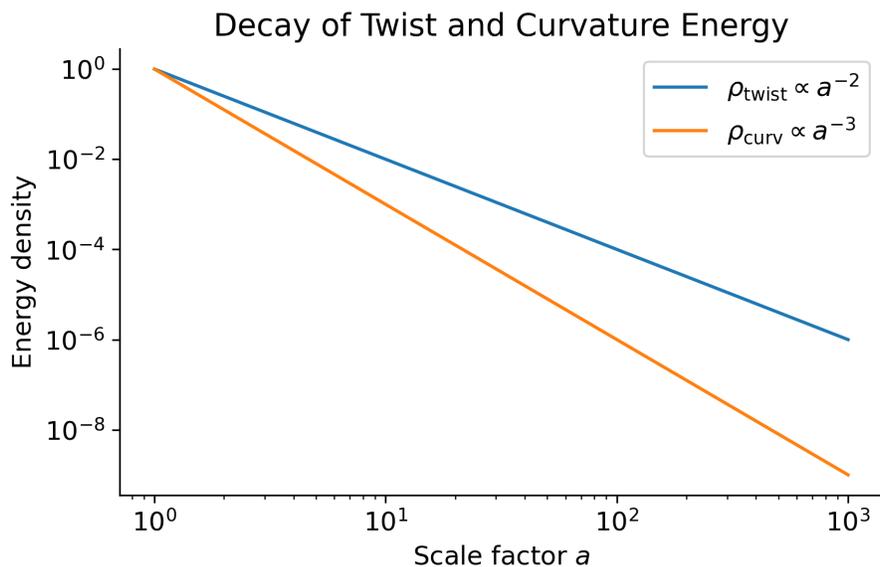


Figure 6: Decay of twist and curvature energy densities as the universe expands.